

Measurements of diffusion coefficient of methane in water/brine under high pressure

Yen-An Chen, Che-Kang Chu, Yan-Ping Chen, Lee-Shin Chu, Shiang-Tai Lin, and Li-Jen Chen *

Department of Chemical Engineering, National Taiwan University, Taipei City, Taiwan

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ABSTRACT

The diffusion coefficient of methane in water plays an important role in the formation and dissociation of methane hydrate. However, most of the previous studies on the diffusion coefficient of methane in brine are performed at room temperature and low pressures, which is quite different from the formation condition of methane hydrate. In this study, we measure the diffusion coefficient of methane in pure water and brine in capillary tube at 10.3 MPa and temperature ranging from 283.15 to 308.15 K. We use the Raman spectrum to measure the ratio of C-H bound signal of methane to the O-H bound signal of water, to estimate the concentration of methane dissolves in water/brine. The Raman spectrum is collected at different time and different positions away from the liquid-gas interface. Diffusion coefficient is determined by fitting the experimental data with the concentration profiles solved from Fick's second law and semi-infinity boundary condition. By this method, we can evaluate the diffusion coefficient at different temperatures or salinities. The diffusion coefficient of methane in water/brine increases as the temperature increases. The diffusion coefficient of methane in brine is lower than that in pure water. Molecular dynamics (MD) simulation is also performed in this study to calculate the diffusion coefficient of methane in water/brine. The MD results can successfully predict the tendency of temperature effect and adding electrolyte.

1. INTRODUCTION

Natural gas hydrate is considered to be a potential unconventional energy resource (Sloan and Koh 2007). The thermodynamic properties of natural gas hydrate have been extensively explored, such as phase boundary (Van Der Waals and Platteeuw 1958; Barrer and Ruzicka 1962a; Dalmazzone et al. 2002; Anderson et al. 2009; Hsieh et al. 2012; Chu et al. 2015, 2016; Juan et al. 2015), volumetric properties (Hester et al. 2007; Manakov et al. 2011; Ning et al. 2015), and dissociation enthalpies (Handa 1986; Rydzy et al. 2007; Gupta et al. 2008). Other physical properties of hydrate had been systematically reviewed (Sloan 1998; Gabbitto and Tsouris 2010). Besides, some studies investigated the reaction kinetics of hydrate formation such as induction time and growth rate (Barrer and Ruzicka 1962b; Pinder 1965; Vysniauskas and Bishnoi 1983; Christiansen and Sloan 1994; Natarajan et al. 1994; Kashchiev and Firooz-

badi 2002a, b, 2003).

It has been pointed out that the formation and dissociation of hydrate is a diffusion-controlled process. Diffusion coefficient of methane in sea water is the controlling parameter in the dissociation process of methane hydrate in seabed sediment (Rehder et al. 2004) and in the migration of methane in marine (Egorov et al. 1999; Lin et al. 2006). Besides, diffusion coefficient of gas is necessary for engineers to carry out the gas-liquid mass transfer calculations and correlations (Himmelblau 1964). Therefore, the diffusion coefficient of methane in brine at the hydrate formation and dissociation condition (i.e., at high pressures) is essential in the engineering process design of methane production out of methane hydrate bearing sediment. There are some measurements on the diffusion coefficient of methane in water in the literature. The capillary cell method incorporated with gas chromatography was applied to measure the diffusion coefficients for methane, ethane, propane and butane in water (Witherspoon and Saraf 1965). Gubbins and coworkers used the diaphragm method to measure the diffusion coefficients

* Corresponding author
E-mail: ljchen@ntu.edu.tw

for gases in water and in brine (Gubbins et al. 1966; Tham et al. 1967; Tham and Gubbins 1972). The diffusion coefficients for gases in liquids have been measured by some other methods, such as the inverted tube method (Maharajh and Walkley 1973), the flow method with pulse injection and detect the dispersion peak by differential refractometer (Pratt et al. 1973), the modified Barrer method (Jähne et al. 1987), and the time-resolved pressure detection method (Sachs 1998). More recently Chou and coworkers proposed a new method to measure the diffusion coefficients for gases (methane, CO₂ and ethane) in water loaded inside a capillary tube at high pressures by using Raman spectroscopy (Lu et al. 2006, 2013; Guo et al. 2013; Lin et al. 2014). However, most of the experimental results of diffusion coefficients for gases in water/brine were performed at atmospheric pressure (Witherspoon and Saraf 1965; Maharajh and Walkley 1973; Pratt et al. 1973; Jähne et al. 1987). Some experimental works of diffusion coefficients were carried out at high pressures, but only limited to gases in pure water (Sachs 1998; Lu et al. 2006; Guo et al. 2013).

In this study, the diffusion coefficients of methane in pure water and in brine are determined at 10.3 MPa and temperature ranging from 283.15 to 308.15 K by using the Raman spectroscopy. Instead of using experimental method of Lu et al. (2006) to assemble a capillary tube for the diffusion coefficient measurement at high pressures, we propose a simplified method to assemble the capillary tube for the Raman spectroscopy measurements.

2. EXPERIMENTAL

2.1 Materials

Water was purified by double distillation and then followed by a PURELAB Maxima Series (ELGA Labwater) purification system with the resistivity always better than 18.2 MΩ·cm. The methane gas was purchased from Praxair with a purity of 99.97%. Electrolytes NaCl, NaBr, NaI, and CaCl₂·2H₂O with a purity of 99.5% were purchased from Merck.

2.2 Experimental Setup

The experimental setup for the measurement of the diffusion coefficient of methane in water/brine under high pressure is schematically illustrated in Fig. 1. Fused silica capillary tube (150 μm inner diameter and 360 μm outer diameter, Polymicro Technologies) with standard polyimide coating was used as the diffusion cell in this study. The capillary tube was cut into 8-cm pieces and the protecting polyimide coating outside the capillary tube was removed by alcohol burner. Water (or brine) was loaded into the capillary tube by dipping one end of the capillary tube into water (or brine). The water (or brine) in the capillary would rise

rapidly due to the capillary force. About half of the capillary tube was filled with liquid and the liquid gas interface is located in the viewing window where the polyimide protecting layer was already removed to make sure the gas-liquid interface could be observed by the CCD camera. The end of the capillary tube with liquid was sealed by acetylene flame and the other end was hooked up with Micro Tight Adapter and then connected to a pressurization system (the syringe pump, Teledyne Isco 65D) via Swagelok connector. The photo of the assembled capillary tube is shown in Fig. 2.

This assembled capillary tube was then mounted onto the temperature control platform with a thermostatted water temperature circulated by thermostatic water bath circulator (Thermo Haake DC30-k20) and the temperature of sample capillary tube was monitored by a Yokogawa TX10 thermal couple with an accuracy of 0.1°C (calibrated by a quartz thermometer, HP2804a, Hewlett-Packard Co.).

The Raman system includes a Raman spectrometer with focal length of 1000 mm (FHR 1000, Horiba), Raman probe (Superhead, Horiba) with Charge-coupled Device (CCD) camera (SYN-1024x256-OE, Synapce), and high power laser (532 nm wavelength and 800 mW), as the part number 6, 7, and 9, respectively, illustrated in Fig. 1. The objective is M Plan Apo SL50x purchased from Mitutoyo, the slit is 300 μm controlled by the spectrometer. The filter is 532 nm laser line filter provided by omega optical. The position of the Raman probe can be controlled by stepping motor with a minimum step of 2.5 μm.

2.3 Spectra Collection

The syringe pump was maintained at 10.3 MPa (= 1500 psi) methane gas. Then the valve between the syringe pump and the capillary tube was open to pressurize the capillary tube up to 10.3 MPa. It took less than 1 minute for the pressure to stabilize at 10.3 MPa. Raman spectrum of methane dissolved in water in the capillary tube was collected as a function of time. Each acquisition time was 50 sec with two accumulations using an 1800 groove mm⁻¹ grating with a spectral resolution of 1 cm⁻¹. The Raman spectrum with wavenumber ranging from 2500 to 3950 cm⁻¹ was collected as demonstrated in Fig. 3. The Raman spectrum was integrated to calculate the peak area. The broad peak ranging from 2750 to 3850 cm⁻¹ was attributed to O-H stretching of water, which can be further deconvoluted into 5 sub-band based on the local hydrogen bond (Sun 2009), and the small peak ranging from 2890 to 2930 cm⁻¹ was attributed to C-H bond in methane (symmetric stretching vibration), as the red area shown in Fig. 3. The ratio of these peak area extracted from Raman spectrum had been extensively applied to quantitatively determine the concentration of certain species in the system (Wopenka and Pasteris 1986). That is, the ratio of these two Raman peak areas is directly proportional to the ratio of concentrations (in mole fraction) of two species.

$$\frac{A_A \sigma_{r,A}(\bar{\nu}_A)}{A_B \sigma_{r,B}(\bar{\nu}_B)} = \frac{C_A}{C_B} \quad (1)$$

Where A_A and A_B are the peak area for a certain vibrational mode of species A and B, respectively, $\sigma_{r,A}(\bar{\nu}_A)$ and $\sigma_{r,B}(\bar{\nu}_B)$ are the relative normalized differential Raman scattering cross section for vibrational mode species A and B, at a wave number $\bar{\nu}_A$ and $\bar{\nu}_B$, respectively, and C_A and C_B are concentration of species A and B, respectively, in mole fraction.

Note that Liu et al. (2012) pointed out that Raman signals of dissolved CO_2 do not correlate strictly linearly any-

more for 1 M NaCl aqueous solution. On the other hand, Caumon et al. (2014) pointed out that the salinity effect on the variation of $\text{CH}_4/\text{H}_2\text{O}$ peak area ratio as a function of methane concentration is negligible when the salinity is low (< 4 m) and the $\text{CH}_4/\text{H}_2\text{O}$ peak area ratio dependence of methane concentration is linear at low methane concentration (< 0.2 m). Therefore, Eq. (1) is applied to determine the methane concentration in the pure water as well as brine system.

Raman spectrum of methane dissolved in water was collected at different times and positions from the methane-liquid interface. For the pure water systems, the Raman spectra

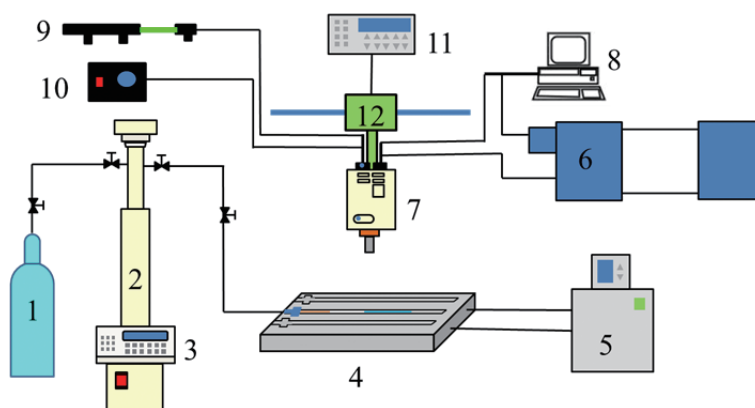


Fig. 1. Schematic diagram of experimental system. (1) Methane cylinder; (2) Syringe pump (Teledyne Isco 65D); (3) Syringe pump controller; (4) Temperature control platform; (5) Thermostatic water bath; (6) Raman spectrometer (FHR 1000, Horiba); (7) Raman probe (SuperHead, Horiba) with Charge-coupled Device (CCD) camera (SYN-1024x256-OE, Synapce) integrated by an X50 objective lens (Mitutoyo); (8) Personal Computer; (9) Laser light source; (10) Video light source; (11) Stepping motor controller; (12) Stepping motor.

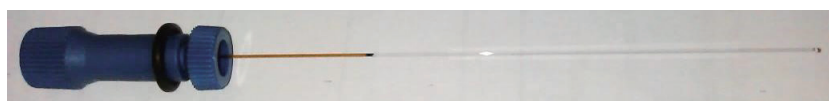


Fig. 2. Photo of an assembled capillary tube. The end on right-hand side was sealed by acetylene flame and the other end (left-hand side) was hooked up with the Micro Tight Adapter.

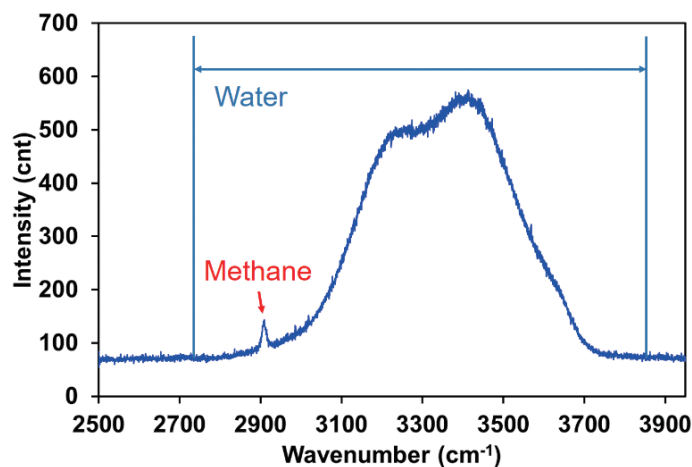


Fig. 3. Raman spectrum of methane dissolved in water.

were collected at 0.250, 0.500, and 0.750 cm away from the gas-liquid interface and at 0.125, 0.250, 0.375, and 0.500 cm away from the gas-liquid interface for the brine systems. The measurement of the time dependence of concentration would be completed within 10 hr usually. The Raman spectrum near the gas-liquid interface (less than 125 μm away from the gas-liquid interface) was measured after three days, which would be treated as the Raman spectrum of saturated methane solution at prescribed system condition (pressure, temperature and salinity). The temperature control platform (part number 4 illustrated in Fig. 1) was housed inside an environmental chamber and the temperature control system would keep working throughout the whole experimental duration.

2.4 One-Dimensional Diffusion

In this study, when the capillary tube is pressurized up to 10.3 MPa by methane, the methane-water (vapor-liquid) interface is generated and initiated to dissolve methane across the interface into water (or brine). Methane then diffuses along the capillary tube driven by the chemical potential gradient, which is proportional to the concentration gradient for ideal mixture (Bird et al. 2007). The combined flux N_{Az} (number of moles of A that go through a unit area in unit time) in z direction can be expressed as,

$$N_{Az} = -cD_{AB} \frac{\partial x_A}{\partial z} + x_A(N_{Az} + N_{Bz}) \quad (2)$$

The solubility of methane in water (or brine) is rather low (Duan and Mao 2006) therefore the advection contribution (second term in the right hand side) caused by diffusion can be neglected (Bird et al. 2007; Incropera et al. 2007). Since the inside diameter of the capillary tube is much smaller than the length of the capillary tube, the diffusion of methane along the capillary tube is assumed to obey the one-dimensional Fick's second law,

$$\frac{\partial C}{\partial t} = \frac{\partial}{\partial z} \left(D \frac{\partial C}{\partial z} \right) \quad (3)$$

where D is the Fickian diffusion coefficient.

There are three boundary conditions used in this study. (1) The concentration of methane at the vapor-liquid interface is assumed to be constant, which is equal to the saturated concentration of methane C_0 at system condition (temperature, pressure, and salinity). (2) The diffusion coefficient of gas in liquid is low, so the penetration length is much smaller than the length of the capillary tube. Therefore, semi-infinity boundary condition is assumed. (3) In addition, there is no methane dissolved into water (or brine) before the system is pressurized (Bodnar and Himmelblau 1962). These three boundary conditions correspond to the

following equations:

$$\begin{cases} C = C_0 \text{ at } z = 0, t > 0 \\ C = 0 \text{ at } z \rightarrow \infty, t > 0 \\ C = 0 \text{ at } t = 0, z \geq 0 \end{cases} \quad (4)$$

The analytical solution of the Eq. (3) with the boundary conditions, Eq. (4), yields a complementary error function (Bodnar and Himmelblau 1962; Welty et al. 2007)

$$\frac{C}{C_0} = \text{erfc}(\eta) \quad (5)$$

where η is a dimensionless term $\eta = \frac{z}{\sqrt{4Dt}}$.

Equation (5) is then applied to determine the diffusion coefficient of methane in water by numerical data regression of the experimental data of methane concentration as a function of time extracted from Raman spectra.

2.5 Molecular Dynamics Simulation

The diffusion coefficient of methane in water and brine is also estimated by molecule dynamics (MD) simulations using GROMACS 4.5 (Berendsen et al. 1995; Van Der Spoel et al. 2005; Pronk et al. 2013). The force field used in this study is OPLS-aa (Jorgensen et al. 1996), except for water where the TIP4P-ICE model is used. The cutoff radii for nonbond interactions is 1 nm. Long range Coulomb interactions are determined using the particle-mesh Ewald (PME) (Darden et al. 1993) method. The simulations are conducted under constant temperature and pressure [isothermal-isobaric (NPT) ensemble]. Nose-Hoover thermostat is applied to control the temperature and Parrinello-Rahman method is applied to the pressure control. The system contains 1000 water molecules, 11 electrolyte atoms, and 6 methane molecules. Periodic boundary condition is applied in all three dimensions. Equation of motion is calculated using leapfrog algorithm with an integration time step of 1 fs. The total simulation time is 100 ns. The diffusion coefficient is calculated every 10 ns after the first 30 ns (equilibration) using the mean square displacement method of the molecules, as shown in Eq. (6).

$$D_s = \frac{1}{6} \lim_{t \rightarrow \infty} \frac{\langle |r(t + \Delta t) - r(t)|^2 \rangle}{\Delta t} \quad (6)$$

where D_s is the self-diffusion coefficient and $r(t)$ is the vector of position.

The self-diffusion diffusion coefficient calculated from Eq. (6) can be converted to Fickian diffusion coefficient by Eq. (7).

$$D_{AB} = (x_A D_B + x_B D_A) \left[1 + \left(\frac{\partial \ln \gamma_A}{\partial x_A} \right) \right] \quad (7)$$

where D_{AB} is Fickian diffusion coefficient of A species in B, x_A and x_B are the mole fraction of component A and B, respectively, D_A and D_B are the self-diffusion coefficient of component A and B, respectively, and γ_A is the activity coefficient of component A.

The differential of activity to concentration is determined by the predictive activity coefficient model, COSMO-SAC model (Hsieh and Lin 2011).

3. RESULTS AND DISCUSSION

3.1 Diffusion Coefficient of Methane in Water at 10.3 MPa (= 1500 psi)

The peak area ratio of methane peak and water peak is divided by that measured at saturated methane condition that yields the dimensionless concentration, defined by methane concentration relative to saturated concentration, C/C_0 . Figure 4 shows variation of the dimensionless concentration of methane in water at three different distances from the vapor-liquid interface as a function of time at 298.15 K. The diffusion coefficient is then determined by least square fitting Eq. (5) to experimental data of dimensionless concentration vs time, as the solid curves illustrated in Fig. 4. Diffusion coefficient ranging from 1×10^{-6} to 5×10^{-4} $\text{cm}^2 \text{s}^{-1}$ is substituted into Eq. (5) and the root mean square deviation is calculated for each diffusion coefficient. The diffusion with the least deviation is the best fitted diffusion coefficient. The uncertainty with 95% confidence is determined by half of distance with double of least deviation (Guo et al. 2013).

A series of experiments of Raman spectroscopy on methane in water loaded in the capillary tube at 10.3 MPa, temperature ranging from 283.15 to 308.15 K were performed, and the results of the diffusion coefficient are listed in Table 1. Figure 5 shows the results of the diffusion coefficient of methane in water in this study in comparison with that of literature data (Witherspoon and Saraf 1965; Gubbins et al. 1966; Tham et al. 1967; Maharajh and Walkley 1973; Pratt et al. 1973; Jähne et al. 1987; Sachs 1998; Lu et al. 2006; Guo et al. 2013). It is obvious that the diffusion coefficient of methane in water rises along with an increase in temperature. It should be noted that some experiments of these previous studies have been performed at atmospheric pressure (Witherspoon and Saraf 1965; Gubbins et al. 1966; Tham et al. 1967; Maharajh and Walkley 1973; Pratt et al. 1973; Jähne et al. 1987) and the others at high pressures (Sachs 1998; Lu et al. 2006; Guo et al. 2013). Figure 5 reveals that the diffusion coefficient is not sensitive to pressure and our experimental results are consistent with that of previous studies within the experimental error. Note that our experimental results have an excellent agreement with

that of Maharajh and Walkley (1973) and Guo et al. (2013). On the other hand, the results of Gubbins et al. (1966) are always slightly larger than our experimental results.

The variation of diffusion coefficient of methane in water as a function of temperature can be described by Eq. (8) (Himmelblau 1964).

$$\ln D / (10^5 \text{ cm}^2/\text{s}) = \frac{A}{T/K} + B \quad (8)$$

where the parameters $A = -1990 \pm 213$ and $B = 7.11 \pm 0.72$ with $R^2 = 0.95$ for our experimental results of methane diffusion coefficient in water, as the red solid curve illustrated in Fig. 5.

On the other hand, the diffusion coefficient can also be predicted by Hayduk and Laudie's (1974) correlation,

$$D_{AB} = \frac{13.26 \times 10^{-5}}{\mu_B^{1.4} V_A^{0.589}} \quad (9)$$

where D_{AB} is Fickian diffusion coefficient of A species in B ($\text{cm}^2 \text{s}^{-1}$), μ_B is the solvent viscosity (cP), V_A is the molar volume at normal boiling point of solute, for methane $V_A = 37.7 \text{ cm}^3 \text{ g}^{-1} \text{ mol}$.

The pressure effect on diffusion coefficient is taken into account via the solvent viscosity in Eq. (9). In general, the pressure dependence of viscosity of liquids is very weak. For example, the difference between viscosities of water measured at 0.1 and 10 MPa in the temperature range 25 - 50°C is always smaller than 0.2% (Schmelzer et al. 2005). Similarly, the pressure dependence of viscosity of NaCl aqueous solution is very weak (Kestin et al. 1978a). Consequently, the pressure effect on diffusion coefficient is weak enough to be neglected.

The viscosity of pure water is calculated by using the correlation of Kestin et al. (1978a, b), which covers the range 273.15 - 313.15 K with an uncertainty of 0.05%. The prediction results of diffusion coefficient of methane in pure water from Eq. (9), as the red dashed line illustrated in Fig. 5, are consistent with our experimental results at low temperatures and slightly larger than our experimental results at high temperatures.

3.2 Diffusion Coefficient of Methane in Brine at 10.3 MPa (= 1500 psi)

The diffusion coefficient measurements are also performed for methane in 6.5 wt% CaCl_2 , 3.5 wt% NaCl, 6.0 wt% NaBr, and 8.6 wt% NaI aqueous solution at 10.3 MPa and temperature ranging from 288.15 to 308.15 K. Note that the mole fraction of cation in these electrolyte solutions is fixed at 0.011, a constant value. The experimental results of diffusion coefficient of methane in these electrolyte

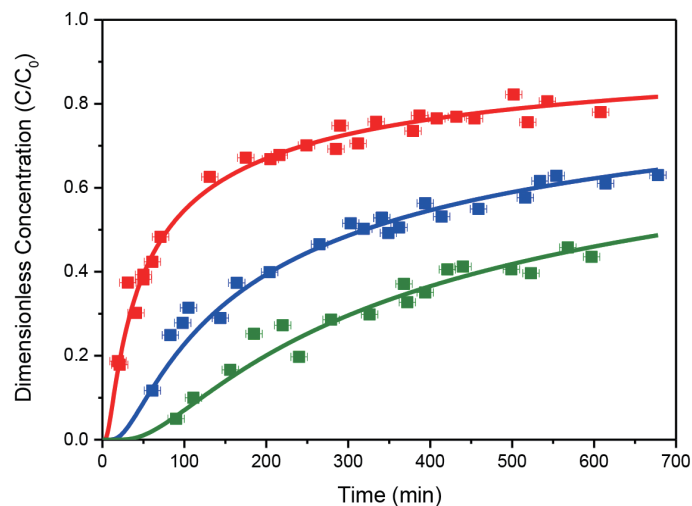


Fig. 4. Dimensionless concentration profiles of the diffusion process of methane in pure water at 298.15 K and 10.3 MPa. Dimensionless methane concentration were determined at 2.50 (■), 5.00 (■), and 7.50 mm (■) from the vapor-liquid interface. Solid curves are the regression results of Eq. (5) with $D = 1.66 \times 10^{-5} \text{ cm}^2 \text{ s}^{-1}$.

Table 1. Experimental results of diffusion coefficient of methane in water.

Temperature (K)	Diffusion coefficient ($\text{cm}^2 \text{ s}^{-1}$)	Uncertainty ($\text{cm}^2 \text{ s}^{-1}$)
283.15	1.12×10^{-5}	2.9×10^{-6}
293.15	1.38×10^{-5}	3.1×10^{-6}
298.15	1.44×10^{-5}	1.1×10^{-6}
303.15	1.71×10^{-5}	3.6×10^{-6}
308.15	2.04×10^{-5}	3.7×10^{-6}

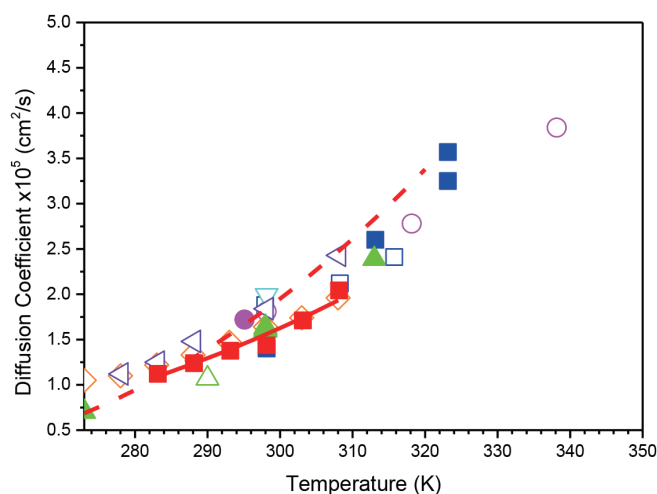


Fig. 5. Comparison of experimental results of diffusion coefficients of methane in pure water in this study with that of literature data. ■, experimental results in this work; ■ (Witherspoon and Saraf 1965); ○ (Gubbins et al. 1966); △ (Pratt et al. 1973); ▽ (Tham et al. 1967); ◇ (Maharajh and Walkley 1973); △ (Jähne et al. 1987); ■ (Sachs 1998); ● (Lu et al. 2006); and ▲ (Guo et al. 2013). Red solid line stands for the calculated results from Eq. (8). Red dashed line represents the prediction results from the correlation of Hayduk and Laudie (1974).

solutions at 10.3 MPa and temperature ranging from 288.15 to 308.15 K are reported in Table 2 and compared with the results of pure water in this study in Fig. 6. All the diffusion coefficients of methane in brine are consistently lower than that in pure water. For the fixed mole fraction of electrolyte, the capability of electrolyte to suppress diffusion coefficient of methane in brine is in the order of $\text{CaCl}_2 > \text{NaI} \sim \text{NaBr} > \text{NaCl}$. That is, the diffusion coefficient of methane in CaCl_2 aqueous solution is the lowest among these electrolyte solutions, and that in NaCl aqueous solution is the highest among these electrolyte solutions. It should be pointed out that the diffusion coefficients of methane in brine at atmospheric pressure measured by Tham and Gubbins (1972), which had a higher concentration of NaCl than that in this study, are higher than the result in this study. However, the diffusion coefficient of methane in pure water measured by the diaphragm method (Gubbins et al. 1966; Tham et al. 1967) is also higher than that measured by Raman spectroscopy in this study and Guo et al. (2013), as mentioned above. Thus, the difference between the results of this study and the results of Tham and Gubbins (1972) might attribute to the systematic deviation between different methods.

On the other hand, the tendency of temperature effect on the diffusion coefficient of methane in brine is rather similar to that in pure water. Therefore, Eq. (8) is also applied to correlate the experimental data and the parameters A and B in Eq. (8) for the diffusion coefficient of methane in these electrolyte solutions are also listed in Table 3.

Hayduk and Laudie's (1974) correlation, Eq. (9), is also applied to predict the methane diffusion coefficient in brine. Viscosity of electrolyte solution is calculated by model of Laliberté (2007) with standard deviation of 3.7%. The dashed lines shown in Fig. 6 stand for the prediction results from Eq. (9). Hayduk and Laudie's correlation successfully predicts the suppression of methane diffusion coefficient due to

addition of electrolyte. However, the diffusion coefficients of methane in brine predicted from Eq. (9) are higher than the experimental results of this work. Besides, the prediction result of adding CaCl_2 is higher than that of adding NaCl , which is also different from the experimental results.

3.3 Comparison with Molecular Dynamics Simulations

The Fickian diffusion coefficient of methane in water and brine calculated by MD simulations is shown in Fig. 6. The calculated diffusion coefficients are found to be consistently lower than experimental values because of the lowered pure water diffusivity using TIP4P-ICE water model. For example, the diffusion coefficient of TIP4P-ICE water is $1.33 \times 10^{-5} \text{ cm}^2 \text{ s}^{-1}$ at 298.15 K, which is about half of the experimental value $2.34 \times 10^{-5} \text{ cm}^2 \text{ s}^{-1}$. Nevertheless, MD simulations correctly provides the relative change of methane diffusivity as a result of change in the electrolytes and temperatures. Other water models may provide higher accuracy in water diffusivity; however, the TIP4P-ICE model has the advantage of providing more accurate ice and hydrate melting temperature and methane solubility in water (Wu et al. 2016). Our results show that the TIP4P-ICE water model can provide useful qualitative information for consistency check with experiments. Considering its efficiency in time and cost, we believe that MD simulations can provide useful information regarding the effect of salt and temperature on methane diffusivity in more complex situations (e.g., mixed electrolytes) before conducting actual experiment.

4. CONCLUSION

The diffusion coefficient of high pressure methane in water and brine is measured in this study. The diffusion coefficient of methane in water measured in this study

Table 2. Experimental results of diffusion coefficient of methane in brine.

solution	Temperature (K)	Diffusion coefficient ($\text{cm}^2 \text{ s}^{-1}$)	Uncertainty ($\text{cm}^2 \text{ s}^{-1}$)
NaCl 3.5 wt%	283.15	1.13×10^{-5}	2.7×10^{-6}
	288.15	1.22×10^{-5}	3.4×10^{-6}
	298.15	1.29×10^{-5}	2.9×10^{-6}
	308.15	1.89×10^{-5}	4.5×10^{-6}
CaCl_2 6.5 wt%	283.15	6.17×10^{-6}	1.8×10^{-6}
	288.15	7.97×10^{-6}	1.9×10^{-6}
	298.15	1.11×10^{-5}	3.7×10^{-6}
NaBr 6.0 wt%	288.15	8.87×10^{-6}	1.7×10^{-6}
	298.15	1.21×10^{-5}	3.7×10^{-6}
	308.15	1.49×10^{-5}	3.9×10^{-6}
NaI 8.6 wt%	288.15	9.22×10^{-6}	2.7×10^{-6}
	308.15	1.46×10^{-5}	6.1×10^{-6}

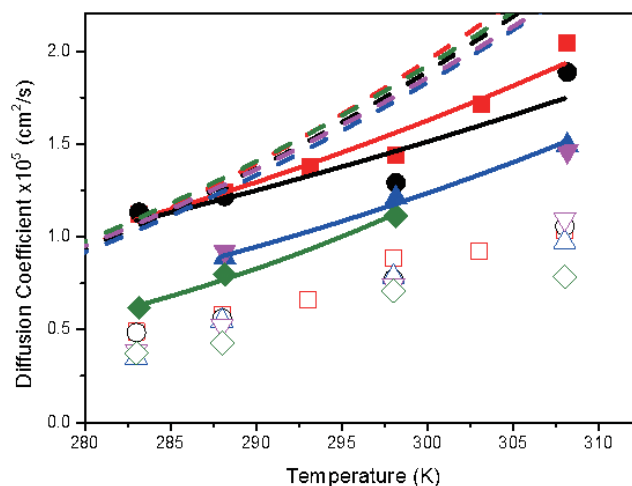


Fig. 6. Diffusion coefficients of methane in water and in brine determined by Raman spectroscopy experiments and MD simulations. Experimental results of diffusion coefficient of methane in pure water (■, red solid and dashed line), in 3.5 wt% NaCl solution (●, black solid and dashed line), in 6.0 wt% NaBr solution (▲, blue solid and dashed line), in 8.6 wt% NaI solution (▼, magenta dashed line), and in 6.5 wt% CaCl₂ solution (◆, green solid and dashed line). MD simulation results of diffusion coefficient of methane in 3.5 wt% NaCl solution (○), in 6.0 wt% NaBr solution (△), in 8.6 wt% NaI solution (▽), and in 6.5 wt% CaCl₂ solution (◇). The solid line stand for the calculated results from Eq. (8) for the methane diffusion coefficients in pure water and in brine. The dashed lines represent the prediction results from the correlation of Hayduk and Laudie (1974) for the methane diffusion coefficients in pure water and in brine.

Table 3. Regressed parameters of the diffusion coefficient of methane in pure water and brine for Eq. (8).

Brine	A	B	R ²
Pure Water	-1990 ± 213	7.11 ± 0.72	0.945
3.5 wt% NaCl	-1670 ± 521	5.98 ± 1.77	0.755
6.5 wt% CaCl ₂	-3260 ± 332	11.0 ± 1.15	0.979
6.0 wt% NaBr	-2320 ± 211	7.94 ± 0.71	0.984

consist to previous result. And the results in brine reveal that the diffusion coefficient of methane will decrease when the electrolyte is added into water. At the same mole fraction, the diffusion of methane in CaCl₂ aqueous is lower than that in NaCl aqueous. The result from molecular dynamic also obtain the same tendency on the effect of temperature and addition of electrolyte.

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